

October 19th, 2017

All-City Tutors: Helping Elementary Students Make Sense of Math

Jim Meyer
Curriculum Specialist
Seattle Public Schools
kjmeyer@seattleschools.org

Goals:

- ❖ **Explore how students are learning math in school.**
- ❖ **Support students' sense-making through questioning.**
- ❖ **Help students incorporate Mathematician into their identity.**

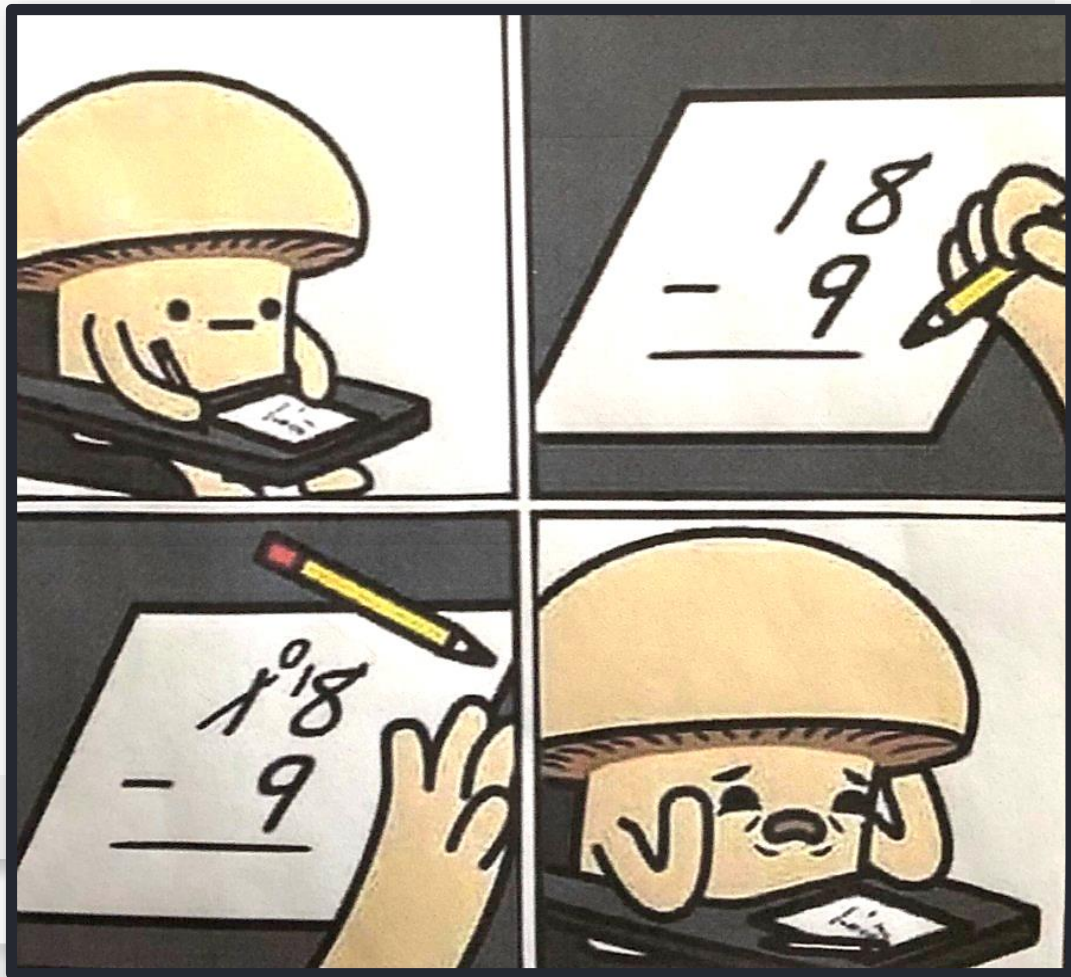
What is CGI?

Caroline La Haie
Park Western Place Es

Meeting students where they are, helping them to build on to their learning, sharing and collaborating with others, making their thinking known to others, revising and verifying their ideas. Children making sense of mathematics.



“CGI is a student-centered approach to teaching math that builds on children’s intuitive ideas for solving math problems or tasks and in which the primary role of the teacher is that of a listener, facilitator, and strategic questioner.”



Math Routines: Choral Count

**Skip Count by 5
starting at 16**

1

—

2

3

—

2

5

/

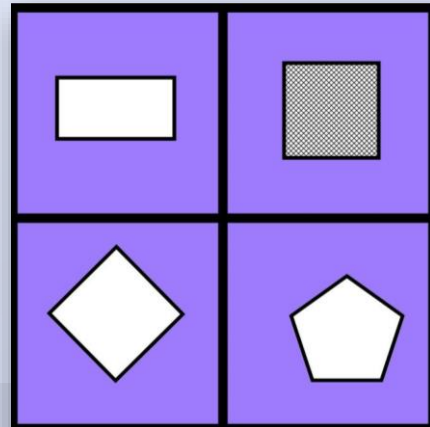
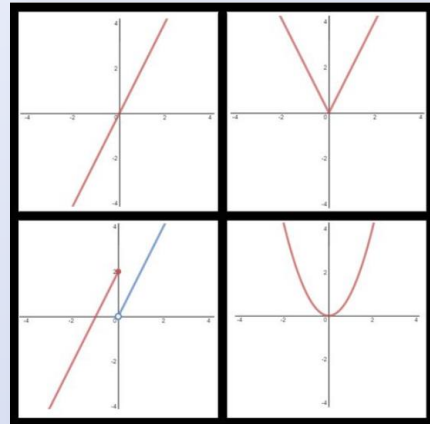
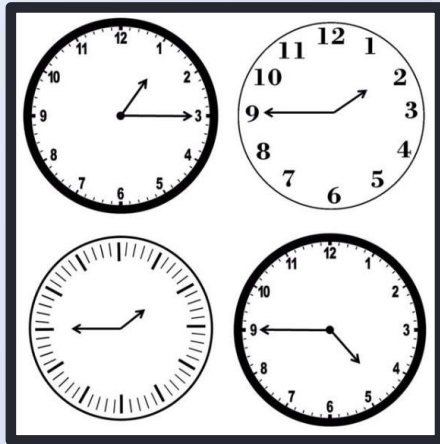
8

2

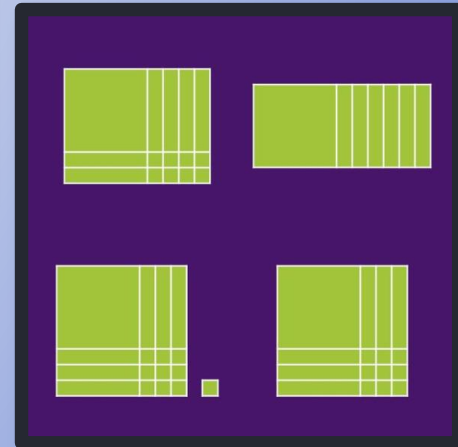
—

6

3	27
123	31



$y = 4x$	$y = x + 7$
$y = -2x + 4$	$y = 3x - 1$



Correct answers are still valued and expected

- Sometimes the goal of a lesson isn't to find the answer.
- Sometimes the goal of a lesson is to understand features of a number system and how they work together.
- Sometimes we want to provide students opportunities to think freely about what is going on in a low stakes situation.

**Algorithms are still taught
and fluency expected.**

Just not taught as early as you might expect

Standard Algorithms

- ❑ **Multi-digit Addition & Subtraction: 4th grade**
- ❑ **Multi-digit Multiplication: 5th Grade**
- ❑ **Multi-digit Division: 6th Grade**

Why not teach the algorithm first?

What are they doing before they learn it?

Number Talk.

What is 6×16

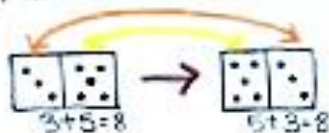
Zero Facts

$$\underline{12} + 0 = \underline{12}$$

$$0 + \underline{12} = \underline{12}$$

Any number + 0 = ^{same} number
No change!

Turn-Around Facts



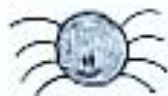
Flip the addends...
The sum DOESN'T change!
 $3+5 = 5+3$

Counting On



* Put the bigger number in your head
then count up!
+1, +2, +3 facts

Doubles



$$4 + 4 = 8$$

the same number is added
together!

My Addition Strategies Mat

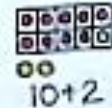
Near Doubles

4 is near 4
 $\begin{array}{r} 4 \\ + 5 \\ \hline ? \end{array}$ $\begin{array}{r} 4 \\ + 4 \\ \hline 8 \end{array}$
So...
Add 1 to
the doubles fact!
 $8 + 1 = 9$

Make A Ten

$$9 + 3 = ?$$

Think:



Part-Part-Whole



Part + Part = Whole

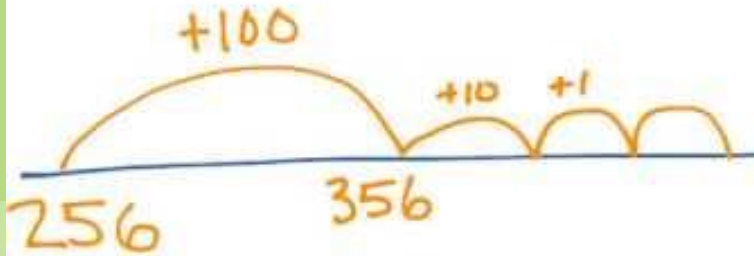
Combine Numbers

$$\textcircled{8} + 5 + \textcircled{2} = ?$$

$\begin{array}{r} 8 + 2 = 10 \\ \hline 10 + 5 = 15 \end{array}$

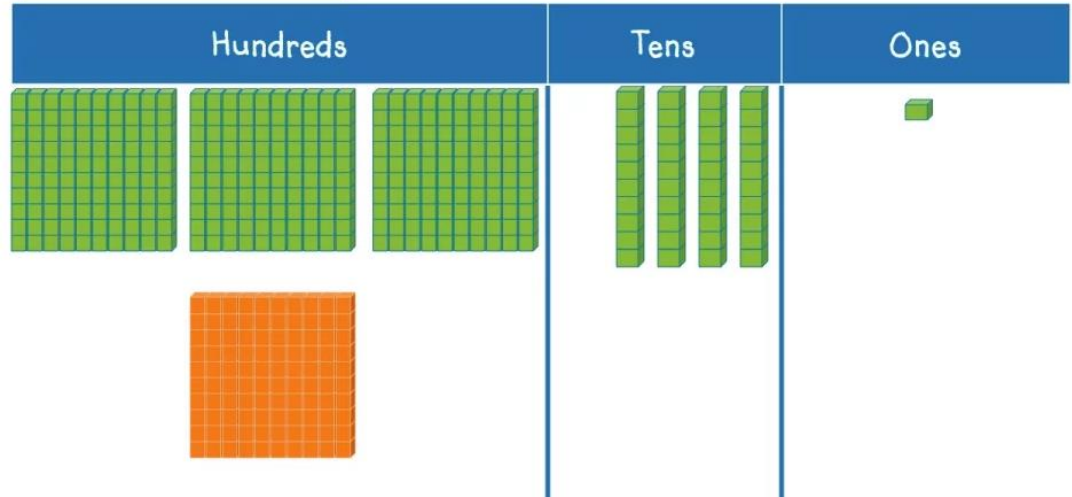
Open Number Line

$$256 + \underline{137} =$$



Core Lesson

What is $341 + 156$?



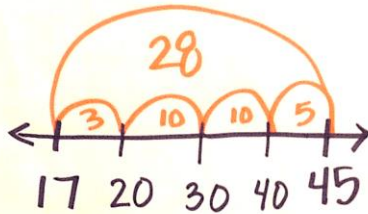
I can subtract two-digit numbers.

$$45 - 17$$

Think Addition

$$\begin{aligned} 17 + 3 &= 20 \\ 20 + 20 &= 40 \\ 40 + 5 &= 45 \end{aligned}$$

28

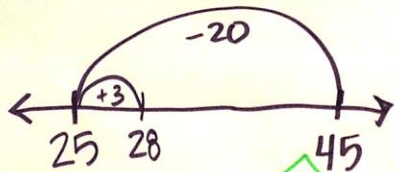


Use negatives

$$\begin{array}{r} 45 \\ - 17 \\ \hline 30 \\ - 2 \\ \hline 28 \end{array}$$

Compensation

$$\begin{aligned} 45 - 20 &= 25 \\ 25 + 3 &= 28 \end{aligned}$$



Decompose a Ten


$$\begin{array}{r} 45 \\ - 17 \\ \hline 28 \end{array}$$

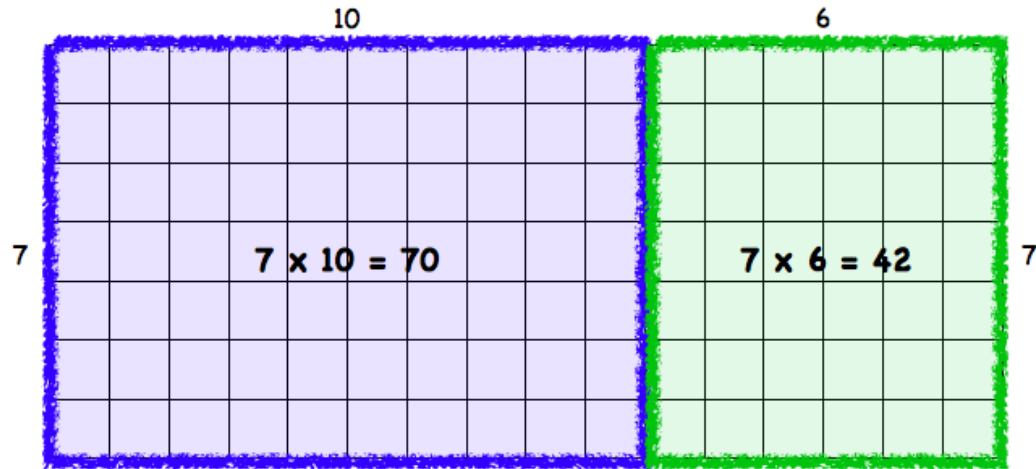
Annotations:
- A blue arrow points from the 5 in 45 to the 5 in 15 (of 30+15).
- A blue arrow points from the 1 in 17 to the 1 in 7 (of 10+7).
- A green arrow points from the 10 in 30 to the 10 in 20 (of 20+8).
- A green arrow points from the 7 in 7 to the 8 in 8 (of 20+8).

Shortcut

$$\begin{array}{r} 3 \ 15 \\ 45 \\ - 17 \\ \hline 28 \end{array}$$

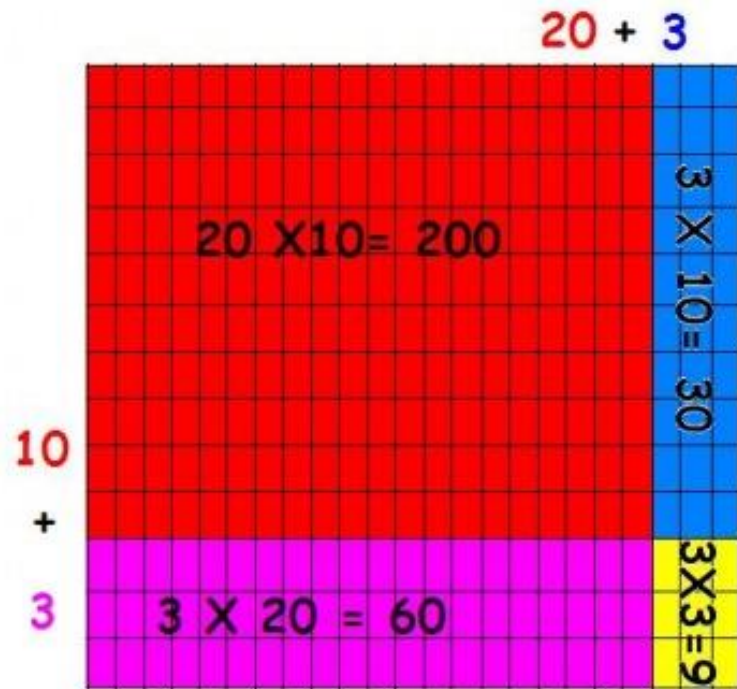
$$7 \times 16 =$$

$$7 \times (10 + 6) =$$




$$70 + 42 = 112$$

13×23



$$\begin{array}{r} 13 \\ \times 23 \\ \hline \end{array}$$

$9 = 3 \times 3$

$30 = 3 \times 10$

$60 = 20 \times 3$

$200 = 20 \times 10$

 299

$$143 \times 27$$

	100	40	3
20	2,000	800	60
7	700	280	21

$$3,180 \div 15 = 213$$

	200	10	3	
15	3,000	150	30	15

3,180	
<u>-3,000</u>	200
180	
<u>- 150</u>	10
30	
<u>- 30</u>	3
0	<u>213</u>



People value what makes sense.

Our number 1 standard of Math Practice is: Make sense of problems and persevere in solving them.

A school bought some math books and 4 times as many science books. The cost of a math book was \$12. A science book cost \$8. Altogether the school spent \$528.

How many science books did they buy?

Make Sense of a Problem and Persevere in solving them. (SMP 1)

Read three times.

- **What is the problem about ? What is happening? Understand the story and context**
- **Read again looking for just the question – what is the purpose of our problem solving.**
- **Read a third time looking for mathematically relevant information.**

Identify Quantities and Relationships (SMP 2)

Sara has 7 cookies

Jeff ran $\frac{1}{2}$ mile.

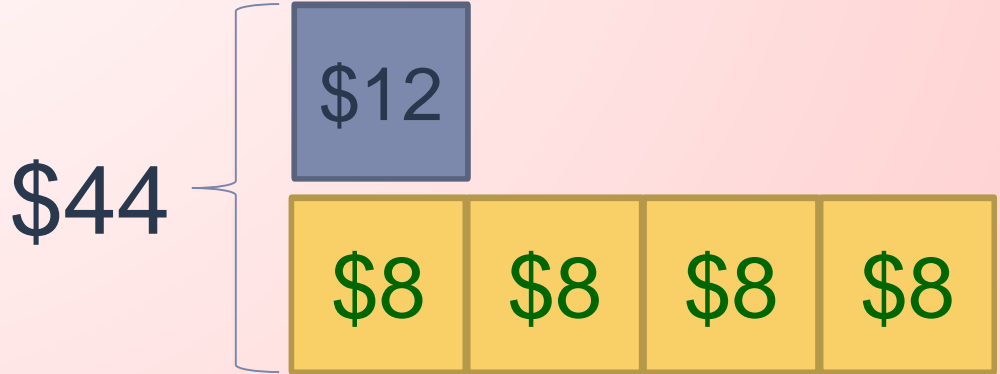
Catherine has 7 fewer
cookies than Sara

Jim ran $\frac{1}{2}$ as far as
Jeff.

Understand the Structure of a problem (SMP 7)

Have I seen a problem that acts like this before... What is happening in this problem.

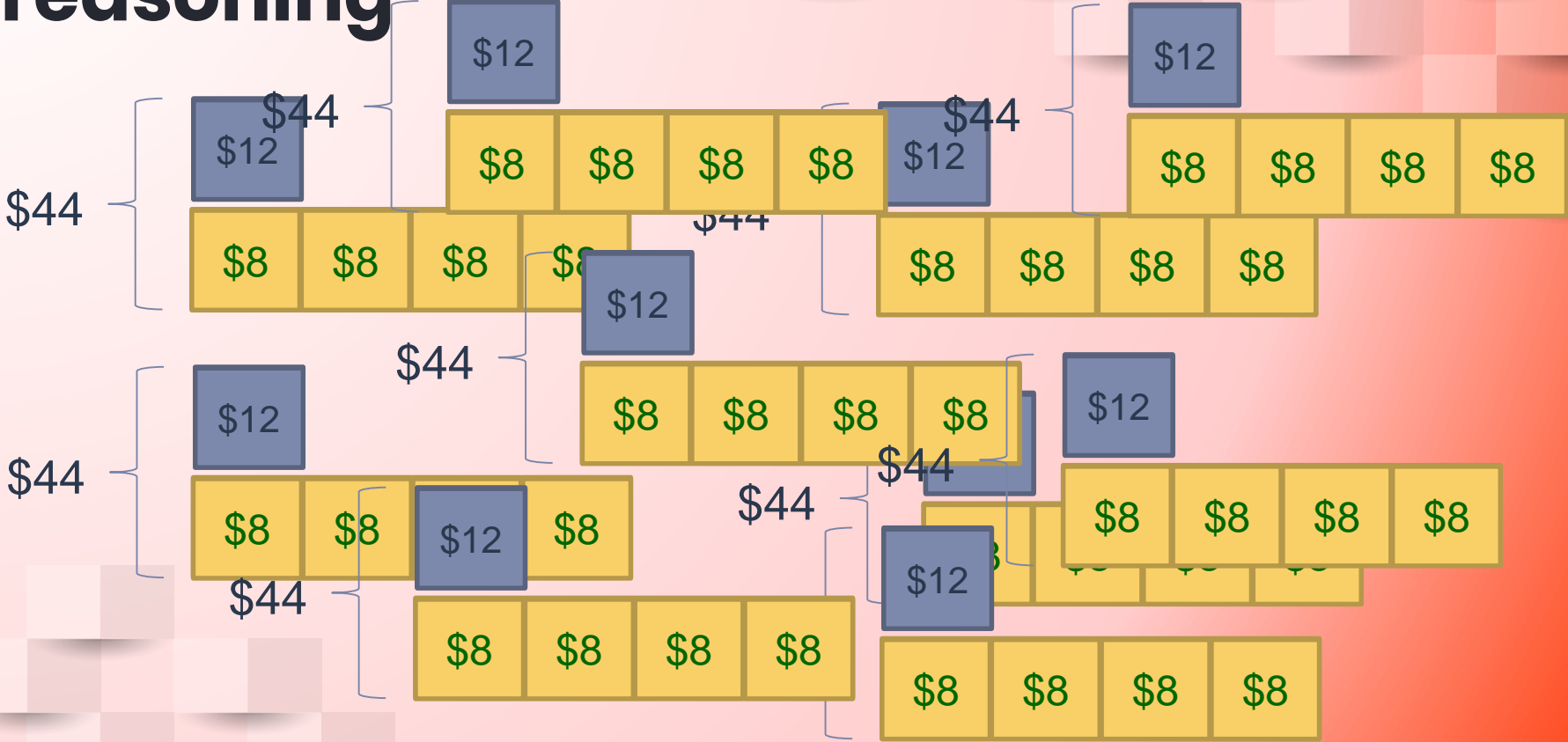
Understand the Structure of a problem



Look for regularity and repeated reasoning (SMP 8)

**Think about what you are doing
over and over to establish
procedure**

Look for repeated reasoning



Look for regularity and repeated reasoning (SMP 8)

Think about what you are doing over and over to establish procedure

$$2+2+2+2+2 = 10$$

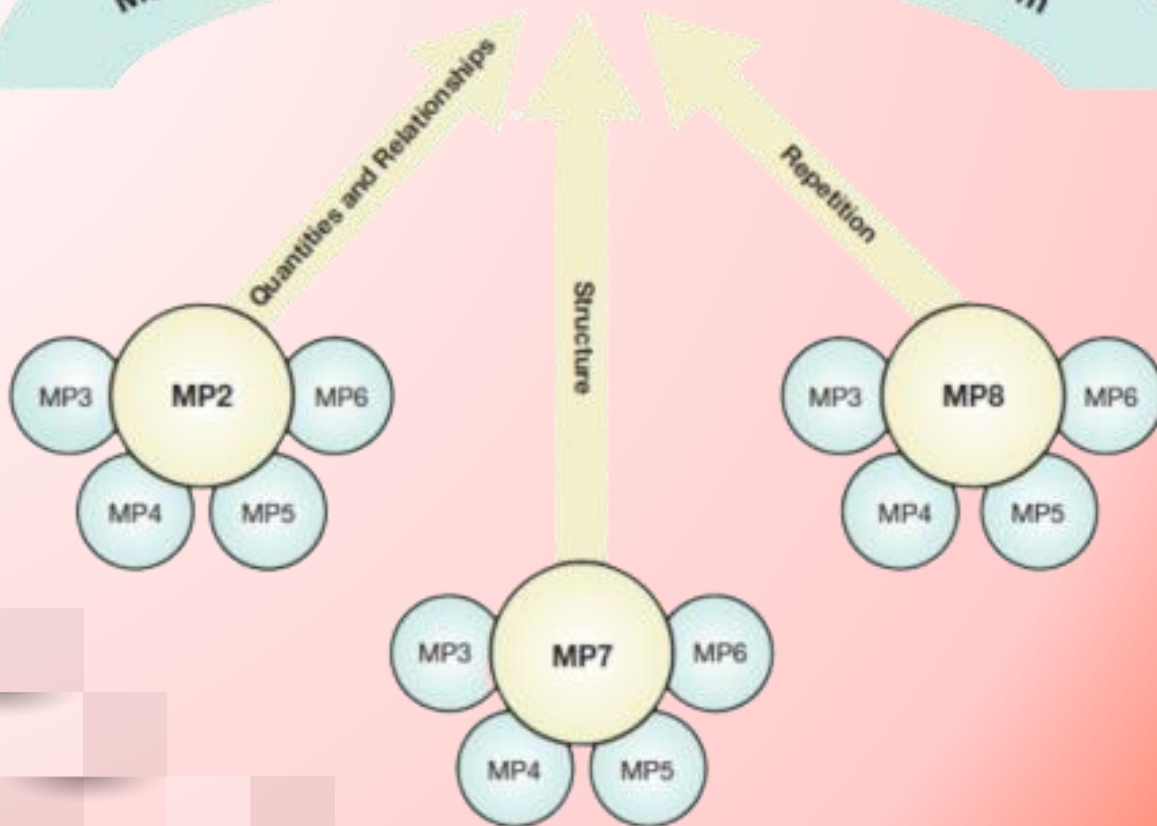


$$\frac{3}{8} + \frac{2}{4} = ?$$

$$\frac{3}{8} = \frac{1}{8} + \frac{1}{8} + \frac{1}{8}$$

$$\frac{1}{8} + 2 \times \frac{1}{8} + 5 \times \frac{1}{8} = \frac{3}{24}$$

MP1
Make Sense of Problems and Persevere in Solving Them



Growth Mindset and Identity

How can we help young people see themselves as capable mathematicians?

Take one minutes to write down what you know or have heard about the idea of “growth mindset.”

Fostering a Growth Mindset

Fixed Mindset

intelligence is static

- **Challenges** ... avoid
- **Obstacles** ... give up
- **Effort** ... no point
- **Criticism** ... deflect
- **Success of others** ...
feel threatened



Growth Mindset

intelligence is developing

- **Challenges**... embraces
- **Obstacles** ... fortitude
- **Effort** ... work hard
- **Criticism** ... learns
- **Success of others** ...
celebrates

Growth Mindset for Mentors

60 minute online module

www.mindsetkit.org

Topic 1: What is a Growth Mindset?

Topic 2: [How Mentors Support Growth Mindset](#)

Topic 3: Key Strategy: Using Growth Mindset Language

Topic 4: Key Strategy: Reframing Challenges, Failures, and Mistakes

Topic 5: Additional Tips and strategies

Changing Mindset:

Questions & Feedback

- Questions support students in sense-making**
- Feedback prompts to support students when they**
 - Struggle**
 - Are making progress**
 - Succeed**

Using Growth Mindset Language and Fostering Math Practices

You and a partner will work on a math problem. One partner plays the student, and the other plays the tutor.

Use the last three pages to determine the situation and develop a response

Students have not yet developed a growth mindset, so the tutor will help the student reframe things in growth mindset language. Use your handouts to help you!

The driver of the 48 bus drives for 8 hours each day. They drive a route that is 18 miles long and ends at the same place it starts – the intersection of MLK and Rainer Avenue. 2 times each hour, how many miles did they drive in one day?

Questions?

Thank you for coming!

Jim Meyer

Math Curriculum Specialist

kjmeyer@seattleschools.org

INSTRUCTIONS FOR USE

EDIT IN GOOGLE SLIDES

Click on the button under the presentation preview that says **"Use as Google Slides Theme"**.

You will get a copy of this document on your Google Drive and will be able to edit, add or delete slides.

You have to be signed in to your Google account.

EDIT IN POWERPOINT®

Click on the button under the presentation preview that says **"Download as PowerPoint template"**. You will get a .pptx file that you can edit in PowerPoint.

Remember to download and install the fonts used in this presentation (you'll find the links to the font files needed in the [Presentation design slide](#))

More info on how to use this template at www.slidescarnival.com/help-use-presentation-template

This template is free to use under [Creative Commons Attribution license](#). You can keep the Credits slide or mention SlidesCarnival and other resources used in a slide footer.



BIG CONCEPT

Bring the attention of your audience over a key concept using icons or illustrations

HELLO!

I am Jayden Smith

I am here because I love to give presentations.

You can find me at @username



1.

TRANSITION HEADLINE

Let's start with the first set of slides

**“Quotations are
commonly printed as a
means of inspiration and
to invoke philosophical
thoughts from the
reader”**

THIS IS A SLIDE TITLE

- ❑ Here you have a list of items
- ❑ And some text
- ❑ But remember not to overload your slides with content

Your audience will listen to you or read the content, but won't do both.

YOU CAN ALSO SPLIT YOUR CONTENT

White

Is the color of milk and fresh snow, the color produced by the combination of all the colors of the visible spectrum.

Black

Is the color of coal, ebony, and of outer space. It is the darkest color, the result of the absence of or complete absorption of light.

IN TWO OR THREE COLUMNS

Yellow

Is the color of gold, butter and ripe lemons. In the spectrum of visible light, yellow is found between green and orange.

Blue

Is the colour of the clear sky and the deep sea. It is located between violet and green on the optical spectrum.

Red

Is the color of blood, and because of this it has historically been associated with sacrifice, danger and courage.

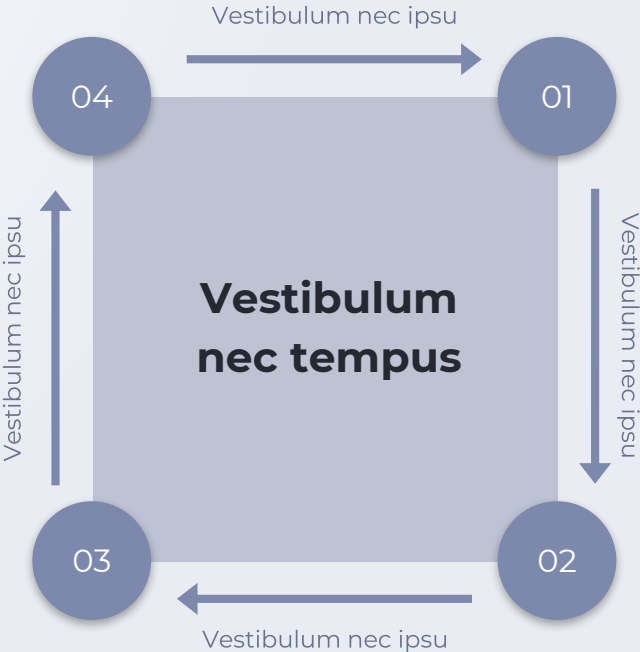
A PICTURE IS WORTH A THOUSAND WORDS

A complex idea can be conveyed with just a single still image, namely making it possible to absorb large amounts of data quickly.



WANT BIG IMPACT?
USE BIG IMAGE.

USE DIAGRAMS TO EXPLAIN YOUR IDEAS



AND TABLES TO COMPARE DATA

	A	B	C
Yellow	10	20	7
Blue	30	15	10
Orange	5	24	16

MAPS



89,526,124

Whoa! That's a big number, aren't you proud?

89,526,124\$

That's a lot of money

185,244 users

And a lot of users

100%

Total success!

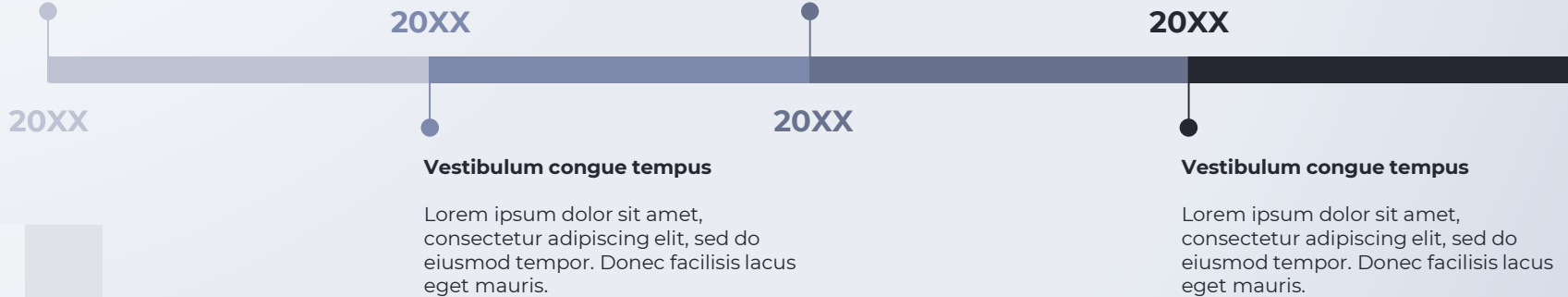
OUR PROCESS IS EASY

Vestibulum congue tempus

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor. Donec facilisis lacus eget mauris.

Vestibulum congue tempus

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor. Donec facilisis lacus eget mauris.



LET'S REVIEW SOME CONCEPTS

Yellow

Is the color of gold, butter and ripe lemons. In the spectrum of visible light, yellow is found between green and orange.

Yellow

Is the color of gold, butter and ripe lemons. In the spectrum of visible light, yellow is found between green and orange.

Blue

Is the colour of the clear sky and the deep sea. It is located between violet and green on the optical spectrum.

Blue

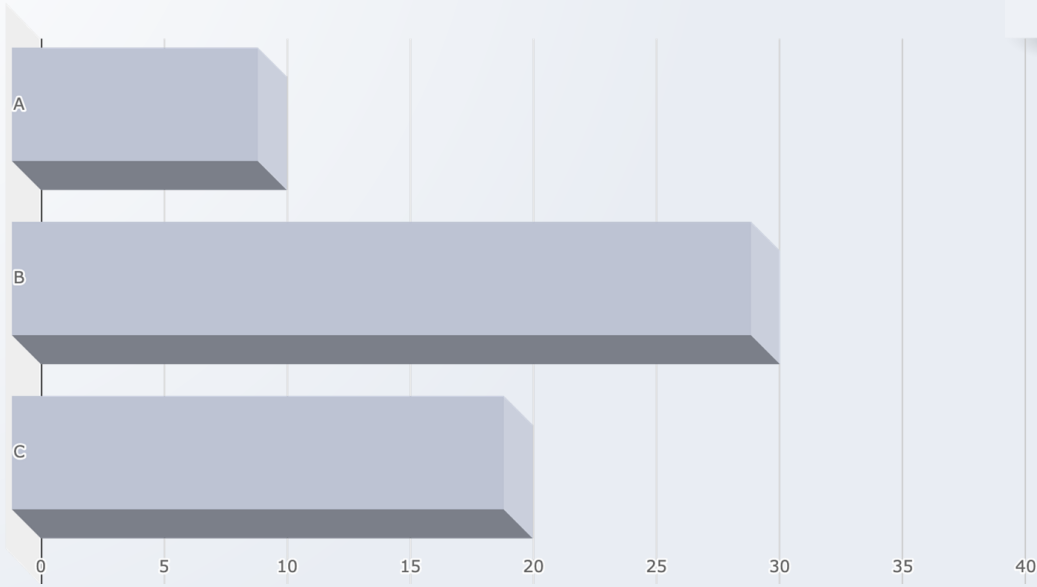
Is the colour of the clear sky and the deep sea. It is located between violet and green on the optical spectrum.

Red

Is the color of blood, and because of this it has historically been associated with sacrifice, danger and courage.

Red

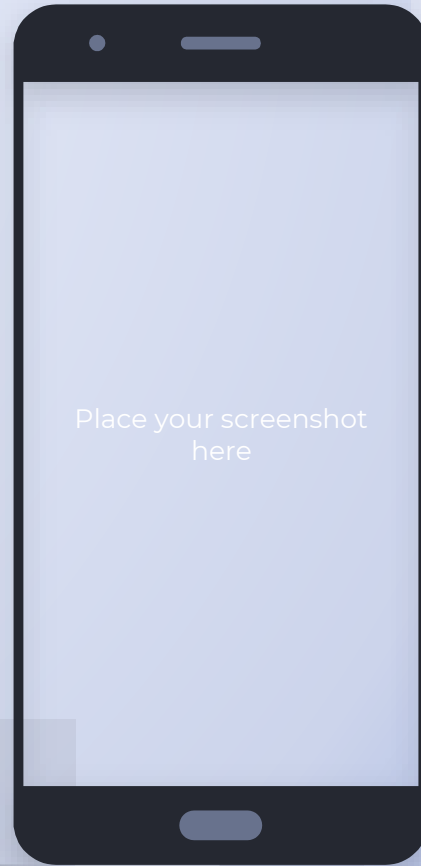
Is the color of blood, and because of this it has historically been associated with sacrifice, danger and courage.



You can insert graphs from [Google Sheets](#)

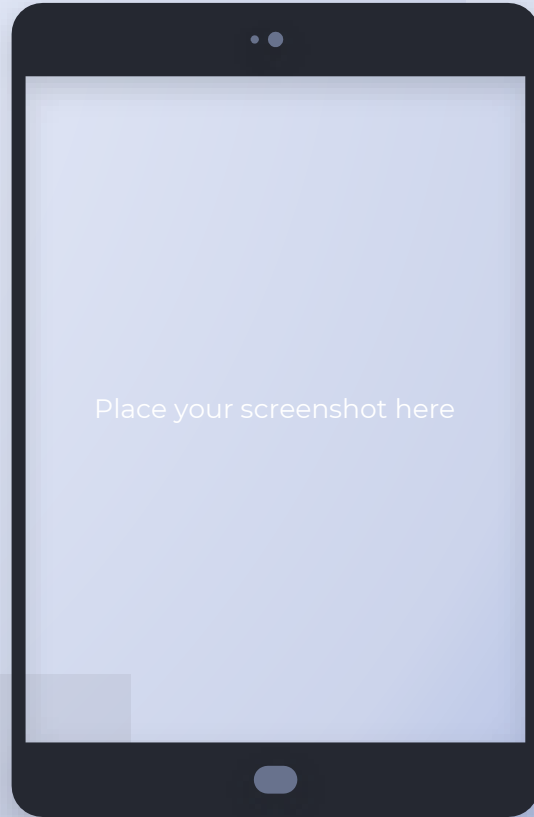
MOBILE PROJECT

Show and explain your web, app or software projects using these gadget templates.



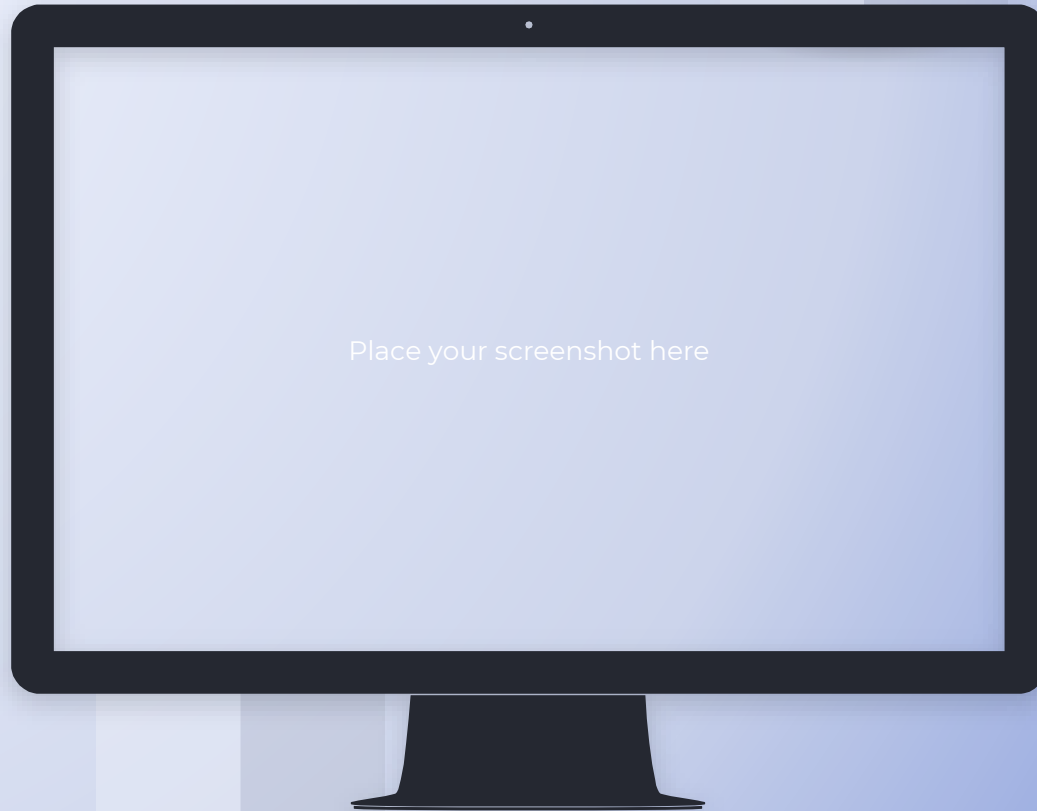
TABLET PROJECT

Show and explain your web, app or software projects using these gadget templates.



DESKTOP PROJECT

Show and explain your web, app or software projects using these gadget templates.



THANKS!

Any questions?

You can find me at:

- @username
- user@mail.me

CREDITS

Special thanks to all the people who made and released these awesome resources for free:

- ❑ Presentation template by [SlidesCarnival](#)
- ❑ Photographs by [Unsplash](#)

PRESENTATION DESIGN

This presentation uses the following typographies:

- ❑ Titles: Poppins
- ❑ Body copy: Montserrat

Download for free at:

<https://www.fontsquirrel.com/fonts/poppins>

<https://www.fontsquirrel.com/fonts/montserrat>

You don't need to keep this slide in your presentation. It's only here to serve you as a design guide if you need to create new slides or download the fonts to edit the presentation in PowerPoint®



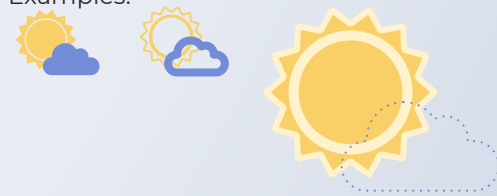
SlidesCarnival icons are editable shapes.

This means that you can:

- Resize them without losing quality.
- Change fill color and opacity.
- Change line color, width and style.

Isn't that nice? :)

Examples:





You can also use any emoji as an icon!

And of course it resizes without losing quality.

How? Follow Google instructions

<https://twitter.com/googledocs/status/730087240156643328>



Slides Carnival

Free templates for all your presentation needs



For PowerPoint and
Google Slides



100% free for personal
or commercial use



Ready to use,
professional and
customizable



Blow your audience
away with attractive
visuals